



Computer Science 252

Problem Solving with Java

The College of Saint Rose
Spring 2016

Topic Notes: Collections

Our next major topic involves additional common mechanisms for naming collections of items.

Motivation for Collections

Sometimes we have a lot of very similar data, and we would like to do similar things to each datum. For example, suppose we wanted to extend our “Drag2Shirts” example to have 4 shirts instead of just 2.

See Example: Drag2Shirts

We could go through the program and everywhere we see `redShirt` and `blueShirt`, add 2 more variables and 2 more segments of code to deal with the new 2 shirts.

See Example: Drag4Shirts

That was not terribly painful, but a bit tedious and error prone. Now, what if we wanted to create 10, 20, or 100 shirts to be dragged around the canvas. We’d want a better way to name the shirts as a group.

We could create a recursive data structure to hold our `TShirt` objects like we did in some recent examples. This is a useful approach in many cases, but we will now consider some other very common ways to manage collections of objects.

Java and other programming languages provide a number of mechanisms to help here. We will consider two in Java. First, we will look at a Java class called the `ArrayList`, and later a lower-level construct common to most modern programming language called *arrays*. Each allows us to use one name for an entire collection of objects.

The Java `ArrayList` Class

Those of you who will go on to take data structures will learn about a variety of ways that collections of data can be stored that vary in complexity, flexibility, and efficiency. We will consider just one of those structures here: the `ArrayList`.

`ArrayList` is a class that implements an *abstract data type* provided by the standard Java utility library.

Let’s see how to use them through an example: we will replace the 4 names of `TShirt` objects in the “Drag4Shirts” example with a single `ArrayList` that holds all 4.

See Example: Drag4ShirtsArrayList

This program has the same functionality, but the 4 variables for the TShirts has been replaced by a single collection, an `ArrayList` of TShirt objects.

We consider each change that was made to the program to see the basic usage of an `ArrayList`.

- First, we need to add an `import` statement to the top of our program.

```
import java.util.ArrayList;
```

This allows us to use the class name `ArrayList` in the rest of the file and Java will know we mean to use the one in the `java.util` package.

- Next, we declare an instance variable for our `ArrayList`:

```
private ArrayList<TShirt> shirts;
```

This looks a little different than any variable declaration we have seen before. Since an `ArrayList` can be used to hold objects of any type, we need to tell Java what type of objects will be stored in this particular `ArrayList`. In this case, it's TShirts. So we place that type inside the `<` and `>`. This is called a *type parameter*.

- Like most Java classes, we need to construct an instance of the class in order use it. This is done in the first statement of the `begin` method:

```
shirts = new ArrayList<TShirt>();
```

This is much like other constructions we have seen, but we again need to include the type parameter so Java will give us an `ArrayList` that is set up to hold a collection of TShirt objects.

- The TShirt instances are then created, and we need to insert each into the `ArrayList`. This is done with the `add` method:

```
shirts.add(shirt);
```

This will take the TShirt named `shirt` and add it to the first available slot in the `ArrayList` named `shirts`.

Note that in this case, we are not requesting any specific location within the `ArrayList` for the shirt. We will later see that we can be more specific here.

Note also that we as users of the `ArrayList` do not know (though when you take data structures, you'll have a pretty good idea) of what's going on inside the `ArrayList` to add the shirt. We just know that it knows how to do it.

When we're done with `begin`, the `ArrayList` contains references to 4 TShirt objects.

- In the `onMousePress` and `onMouseExit` methods, we need to access the `TShirt` objects within the `ArrayList`. We do this with the `get` method:

```
TShirt shirt = shirts.get(shirtNum);
```

Here, `shirtNum` is a loop index variable that will range from 0 to one less than the number of items in the `ArrayList`. We know in this case that there are 4 items, but we can get that information from the `ArrayList` itself using the `size` method, as done in the `for` loops:

```
for (int shirtNum = 0; shirtNum < shirts.size(); shirtNum++)
```

What we see here is that the `ArrayList` has assigned a number, often called an *index*, to each `TShirt` we added to the `ArrayList`, and we can pass that number to the `get` method to get back a specific `TShirt` from the `ArrayList`.

It turns out that the first item we add is given index 0, the next is given index 1, and so on. If we later wanted to get at the first one, we could say:

```
shirts.get(0);
```

but in many cases (like this one), we will access the items within a collection inside a loop, passing in a loop index to the `get` method.

This is our first example of a *search* operation on a collection – we are looking through each object in the collection to find one that contains the `Location`. More precisely, this is a *linear search* and we will say more about this later.

One of the great things about using a construct like an `ArrayList` is that we can extend our programs to keep track of a much larger number of objects. If we want to have 10 `TShirts` on the canvas, we would definitely want to use a collection like an `ArrayList` to keep track of them.

See Example: `Drag10Shirts`

Here, we also place the creation of the `TShirts` into a loop, but just line them up in a row for simplicity. If we wanted them to be organized into rows or to use a fixed set of colors, we would need to use a more complicated loop in the `begin` method. (And we will do just that later.)

If we wanted to create 20 or 50 or 100 `Tshirts`, we could do so by changing the loop in the `begin` method and the remainder of the code does not need to change.

ArrayLists in Custom Objects

One of the challenges we have seen with constructing custom objects with any level of complexity is that we need to have names for all of the graphical objects we construct. When the object includes large numbers of items, ideally created within a loop, an `ArrayList` will come in handy to help keep track of them.

First, we look at a program that doesn't use `ArrayLists`:

See Example: `DrawRoads`

This program draws little segments of roads when we click the mouse. Nothing is new here – we could have written this a while ago.

But now suppose we want to be able to drag one of these around.

We need to have names for all of the components of the road segment so we can do things like move it and check for containment of a point.

See Example: `DragRoads`

The enhancements to the `WindowController` class are all very familiar.

It's in the `RoadSegment` class that we make use of an `ArrayList` to hold the center stripes of our road segment. Notice the same steps: declare a variable with an `ArrayList` type that can hold objects of the appropriate type, construct it with `new`, then add entries with the appropriate types of objects.

In the constructor, we do the construction of the `ArrayList`, then create the actual stripes.

In the `move` method, we loop through the stripes, moving each one.

This is nice, but perhaps we want to combine this functionality with that of the program where we could drag around any of 10 shirts. Let's use an `ArrayList` to keep track of **all** of the road segments we've created, so we can drag **any** segment, not just the most recently drawn one.

See Example: `DragAllRoads`

Here, in addition to having an `ArrayList` to keep track of the components of one of the road segments, we keep an `ArrayList` of `RoadSegment` objects in the `WindowController` class.

Removing from an `ArrayList`

We can augment the last example to remove each road segment from the canvas and from the `ArrayList`. A road segment will be removed if it is being dragged when the mouse leaves the window.

See Example: `DragAllRoadsRemove`

The new functionality is in the `onMouseExit` method of the `DragAllRoadsRemove` class. If the dragging flag is true when the mouse leaves the window, the currently-dragged segment (`selectedSegment`) should be removed. We first remove it from the canvas, then remove it from the `ArrayList`. We also set dragging back to false, since the object we were just dragging no longer exists.

First, we will look at the removal from the list, which is done with the `ArrayList`'s `remove` method. We pass as a parameter the element we want to remove, and if it is an element of the list, it is removed. It is important to note that when we remove an element from an `ArrayList`

with `remove`, any subsequent entries will be “moved up”. That is, if a list contains 5 elements (in positions numbered 0 through 4) and we remove the element at position 2, the `ArrayList` implementation of `remove` will shift the element that was in position 3 into position 2, and the one that was in position 4 into position 3. This means we can still use our `for` loop over the numbers from 0 to `size() - 1` to visit all of our entries. In other words, `remove` does not leave a “hole” at the index from which the element was removed.

The new `removeFromCanvas` method is mostly like the ones we have seen in previous examples: to remove the custom object, we remove each of its components. The difference here is that we need to loop through the `ArrayList`, `get` and then `remove` each element. We also should remove the individual `FilledRects` from the `ArrayList`, which we do all at once with the `clear` method.

We can also remove elements from an `ArrayList` by index rather than value. We will see examples of this soon.

The “for-each” Loop

We have seen that a common task with a collection such as an `ArrayList` is to *iterate* over its contents. That is, “visit” every element in the list exactly once to do something to it.

It is often the case (and was in many of the examples here) that the specific index of an entry in an `ArrayList` is not important as we are iterating over its contents. For example, consider the See Example: `DragAllRoadsRemove` example. It doesn’t actually matter the order in which we process the items in the `ArrayLists` in the `move` and `removeFromCanvas` methods of `RoadSegment` or in the `onMousePress` method of `DragAllRoadsRemove`.

In these cases, the counting `for` loops can be replaced with a related Java construct often called the “for-each” loop.

If we have an `ArrayList` of objects of some type `T` and we wish to loop over all entries in the loop, we can replace a counting loop:

```
ArrayList<T> a = new ArrayList<T>();  
  
...  
  
for (int i = 0; i < a.size(); i++) {  
    T item = a.get(i);  
    // do something with item  
}
```

with a for-each loop:

```
ArrayList<T> a = new ArrayList<T>();  
  
...  
  
for (T item : a) {  
    // do something with item  
}
```

```
for (T item : a) {  
    // do something with item  
}
```

This construct will loop enough times so that the variable `item` will be assigned to each entry in `a` exactly once through the body of the loop.

See Example: `DragAllRoadsForeach`

The for-each construct is not always appropriate, however. For example, in the `findMax` method coming up below, it is more convenient to be able to get the item at position 0 as the initial “max” and then loop over the entries from positions 1 and up to check for larger values.

As you learn more Java, you will see a number of other data structures that can be used with the for-each loop construct.

Other `ArrayList` methods

The examples above demonstrated just a few of the capabilities of the `ArrayList` class: construction, `add`, `get`, `size`, `remove`, and `clear`.

The full documentation for the `ArrayList` can be found at <http://docs.oracle.com/javase/6/docs/api/java/util/ArrayList.html>

Here are a couple of additional methods, some of which will come up in later examples.

- `contains` – determine if a given object is in the list
- `indexOf` – search for first occurrence of a given object in the list and return its index
- `set` – replace the contents at an index with a new element

A few more examples to bring some of this together:

See Example: `MovingFlags`

See Example: `PongBricks`

`ArrayLists` of Primitive Types

Java places a significant restriction on the use of primitive types as the type parameters for generic data structures such as the `ArrayList`. The following would not be valid Java:

```
ArrayList<int> a = new ArrayList<int>();
```

The type in the `<>` must be an object type. Fortunately, Java provides object types that correspond to each primitive type. An `Integer` object is able to store a single `int` value, a `Double` value

is able to store a single `double` value, etc. So the declaration and construction above would need to be:

```
ArrayList<Integer> a = new ArrayList<Integer>();
```

In older versions of Java, programmers would need to be careful to convert back and forth between values of the primitive types and their object encapsulators. To construct an `Integer` from an `int i`, one would need to do so explicitly:

```
a.add(new Integer(i));
```

And to retrieve the `int` value from an `Integer`, one would also do so explicitly:

```
int x = a.get(pos).intValue();
```

However, recent versions of Java automatically convert between the primitive types and their object encapsulating classes. This is called *autoboxing* when converting from primitive to “boxed” encapsulating classes, and *autounboxing* when going back the other way.

So the code above would become

```
a.add(i);
```

and

```
x = a.get(pos);
```

However, the effective programmer should always keep in mind that these conversions are occurring, as there is a computational cost to each.

Another Example

Suppose we have an `ArrayList` of `Integer` values, and someone (by a mechanism which is not our concern) has asked us to write a method that will find the largest value in the `ArrayList`. The following method will achieve this (we assume at least one element in the `ArrayList`):

```
public static int findMax(ArrayList<Integer> a) {  
  
    int max = a.get(0);  
    for (int i=1; i<a.size(); i++) {  
        int val = a.get(i);  
        if (val > max) max = val;  
    }  
    return max;  
}
```

An ArrayList Of and Within a Custom Class

It may or may not have become clear so far that you can use `ArrayLists` in pretty much any context that you can use other data types. Here is one that uses it in two ways:

See Example: `CourseGrades`

In the above example, which you will expand as part of your next lab, `ArrayLists` are used to keep track of a list of students and course grades, and within the class that represents one student's information, the list of the grades.

Java Arrays

The `ArrayList` is a Java class, provided as a standard utility with every Java environment. But it is built on top of a more fundamental programming language construct called an *array*.

In mathematics, we can refer to large groups of numbers (for example) by attaching subscripts to names. We can talk about numbers n_1, n_2, \dots . An array lets us do the same thing with computer languages.

Suppose we wish to have a group of elements all of which have type `ThingAMaJig` and we wish to call the group `things`. Then we write the declaration of `things` as

```
ThingAMaJig[] things;
```

The only difference between this and the declaration of a single item of type `ThingAMaJig` is the occurrence of “[]” after the type.

Like all other objects, a group of elements needs to be created:

```
things = new ThingAMaJig[25];
```

Again, notice the square brackets. The number in parentheses (25) indicates the number of slots to create, each of which can hold one of the elements. We can now refer to individual elements using subscripts. However, in programming languages we cannot easily set the subscripts in a smaller font placed slightly lower than regular type. As a result we use the ubiquitous “[]” to indicate a subscript. If, as above, we define `things` to have 25 elements, they may be referred to as:

```
things[0], things[1], ..., things[24]
```

We start numbering the subscripts at 0, and hence the last subscript is one smaller than the total number of elements. Thus in the example above the subscripts go from 0 to 24.

One warning: When we initialize an array as above, we only create slots for all of the elements, we do not necessarily fill the slots with elements. Actually, the default values of the elements of

the array are the same as for instance variables of the same type. If `ThingAMaJig` is an object type, then the initial values of all elements is `null`, while if it is `int`, then the initial values will all be `0`. Thus you will want to be careful to put the appropriate values in the array before using them (especially before sending message to them! – that’s a `NullPointerException` waiting to happen).

In many ways, and array works like an `ArrayList`, but we will see several differences.

Armed with this new construct, let’s revisit the shirt dragging program to use arrays.

See Example: `Drag10ShirtsArray`

In this code, we we have a single array named `shirts`. This array is declared as an instance variable, constructed at the start of the `begin` method, and given values (references to actual `TShirts`) just after.

Then in the `onMousePress` method, we loop through all of the array entries (as we did previously with an `ArrayList`) to determine which, if any, has been pressed. Finally, in `onMouseExit`, we tell all of the shirts to move back to their starting positions.

Let’s see how this differs from the `ArrayList` version.

- Our instance variable declaration looks a bit different.
- When we construct the array in the `begin` method, we need to tell it how many elements the array will hold (in this case, 10). With the `ArrayList`, we construct a list and we can add as many things to it as we want. The array can only ever hold the number of elements we provided when we constructed it.
- When we add items to the array, we need to specify the index explicitly. There is no way to say “just add it to the end” the way we do with `ArrayLists`.
- When we access array elements, we use the bracket notation in much the same way we use the `get` method of the `ArrayList`.

In this example, we have used an array to keep track of a collection of objects on the canvas. We can also use an array to keep track of the components of a custom object as we did with `ArrayLists`.

An enhancement to this example that shows some of the benefits of arrays, we draw the t-shirts in two rows and use a fixed array of colors for the shirts instead of random colors.

See Example: `Drag10ShirtsNicer`

A few things to notice here:

- We have an array of `Colors` initialized to 10 pre-defined color names that we’ll use for our 10 t-shirts.
- The construction of the t-shirts takes place in a nested loop to make it easier to organize them into 2 rows of 5 shirts each.

Our next enhancement to this example is to draw and drag around 20 shirts, now in 4 rows of 5.

See Example: Drag20Shirts

Most of the program works correctly just by changing the value of the constant `NUM_ROWS` (hooray for constants!). But...the array of colors is not large enough.

We account for this by reusing the colors once we've run out. This is accomplished with some modulo arithmetic:

```
shirts[shirtNum].setColor(shirtColors[shirtNum % shirtColors.length]);
```

Another Example

See Example: DragStudentsS16

Finally, you get to be the stars of a program.

This is just another “drag objects around” example, but this time the objects being dragged are your pictures.

In this example, we place the objects randomly on the canvas, but take some care to make sure they do not overlap at all. Notice the helper method `overlapsAny` that helps ensure this.

Any image being dragged is also made larger while it's being dragged.

Other than that, it's similar to dragging 10 shirts.

Arrays of Non-graphical Types

There is no reason to limit our usage of arrays to graphical object types.

The following is an example of a Java application (rather than an Applet – it starts with a `main` method instead of `begin` and has no graphics canvas) that uses arrays of `String`, `double`, and `int`.

See Example: GradeRangeCounter

There are a few items here we haven't used much this semester (the `Scanner`) but which you have seen before. There are also examples of arrays declared and initialized as `final`, and an example of an array of `int` allocated with `new`.

Inserting and Removing with Arrays

We have already seen that there is quite a bit to keep track of when using arrays, especially when objects are being added. We need to manage both the size of the array and the number of items it contains. If it fills, we either need to make sure we do not attempt to add another element, or reconstruct the array with a larger size.

As a wrapup of our initial discussion of arrays, let's consider two more situations and how we need

to deal with them: adding a new item in the middle of an array, and removing an item from the end.

For these examples, we will not use graphical objects, just numbers. Arrays can store numbers just as well as they can store references to objects.

Suppose we have an array of `int` large enough to hold 20 numbers.

The array would be declared as an instance variable:

```
private int[] a;
```

along with another instance variable indicating the number of `ints` currently stored in `a`:

```
private int count;
```

and constructed and initialized:

```
a = new int[20];  
count = 0;
```

At some point in the program, `count` contains 10, meaning that elements 0 through 9 of `a` contain meaningful values.

Now, suppose we want to add a new item to the array. So far, we have done something like this:

```
a[count] = 17;  
count++;
```

This will put a 17 into element 10, and increment the `count` to 11.

But suppose that instead, we want to put the 17 into element 5, and without overwriting any of the data currently in the array. Perhaps the array is maintaining the numbers in order from smallest to largest.

In this case, we'd first need to "move up" all of the elements in positions 5 through 9 to instead be in positions 6 through 10, add the 17 to position 5, and then increment `count`.

If the variable `insertAt` contains the position at which we wish to add a new value, and that new value is in the variable `val`:

```
for (int i=count; i>insertAt; i--) {  
    a[i] = a[i-1]  
}  
a[insertAt] = val;  
count++;
```

Now, suppose we would like to remove a value in the middle. Instead of “moving up” values to make space, we need to “move down” the values to fill in the hole that would be left by removing the value.

If the variable `removeAt` contains the index of the value to be removed:

```
for (int i=removeAt+1; i<count; i++) {
    a[i-1] = a[i];
}
count--;
```

The loop is only necessary if we wish to maintain relative order among the remaining items in the array. If that is not important (as is often the case with our graphical objects), we might simply write:

```
a[removeAt] = a[count-1];
count--;
```

In circumstances where we are likely to insert or remove into the middle of an array during its lifetime, it usually makes sense to take advantage of the higher-level functionality of the `ArrayList`.

Array and ArrayList Summary

The following list summarizes the key differences and similarities between arrays and `ArrayLists`.

Declaration To declare an array of elements of some type `T`:

```
T[] ar;
```

where `T` can be any type, including primitive types or `Object` types.

And to declare an `ArrayList` that can hold items of type `T`:

```
ArrayList<T> al;
```

where `T` must be an object type. If we want to store a primitive type, we must use Java’s corresponding object wrappers (e.g., `Integer` when we want to store items of type `int`).

Construction To construct (allocate space for) our array of `n` elements of type `T`:

```
ar = new T[n];
```

Once constructed, the array will always have space for n elements of type T – if we want a larger or smaller array, we would have to construct a new one.

The array constructed will have the default value for the datatype stored in each entry. For object types, all entries begin as `null`. For primitive number types, they begin as `0`. For `boolean` arrays, they begin as `false`.

To construct an `ArrayList`:

```
al = new ArrayList<T>();
```

This `ArrayList` initially does not contain any values. Its size will be determined by the number of elements we add to it.

Adding an Element To add an element to an array, we have to specify the position at which we wish to add the new element:

```
ar[i] = t;
```

This will place the item t at position i into our array. i must be in the range 0 to $n-1$ if we constructed our array to have n entries. If there was already some data stored in position i , it will be overwritten with t .

If we want to add the item to the “end” of the array, that is, the first unoccupied slot in the array, we will need an additional variable to keep track of the number of currently-occupied slots. If this is called `aSize`, and we have been careful to make sure the `aSize` elements in the array occupy slots 0 through `aSize-1`, we can add the element with:

```
ar[aSize] = t;  
aSize++;
```

With an `ArrayList`, the `add` method takes care of this:

```
al.add(t);
```

Retrieving an Element To get an item from an array, we use the same notation. To put the value from position i in the array into some variable t :

```
t = ar[i];
```

Whereas with the `ArrayList`, we need to call a method:

```
t = al.get(i);
```

Visiting All Elements To loop over all elements in the array:

```
for (int i=0; i<aSize; i++) {
    t = ar[i];
    // do something with t
}
```

and an `ArrayList`;

```
for (int i=0; i<al.size(); i++) {
    t = al.get(i);
    // do something with t
}
```

In both cases, we can also use the `for-each` loop.

Two-Dimensional Arrays

We can create arrays to hold objects of any type, either basic data types like `int` and `double`, or instances of objects such as `Image` and `FilledOval` or `TShirt`.

Nothing stops us from defining arrays of arrays. To declare an array, each of whose elements is an array of `int`:

```
int[][] twoDArray;
```

While it is normally written without parentheses, we can think of the above declaration as defining `twoDArray` as having type `(int []) []`. Thus each element of `twoDArray` is an array of `ints`.

Despite the fact that Java will treat this as an array of arrays, we usually think about this as a two-dimensional array, with the elements arranged in a two-dimensional table so that `twoDArray[i][j]` can be seen as the element in the i th row and j th column. For example here is the layout for a two-dimensional array `a` with 6 rows (numbered 0 to 5) and 4 columns:

	0	1	2	3
0	<code>a[0][0]</code>	<code>a[0][1]</code>	<code>a[0][2]</code>	<code>a[0][3]</code>
1	<code>a[1][0]</code>	<code>a[1][1]</code>	<code>a[1][2]</code>	<code>a[1][3]</code>
2	<code>a[2][0]</code>	<code>a[2][1]</code>	<code>a[2][2]</code>	<code>a[2][3]</code>
3	<code>a[3][0]</code>	<code>a[3][1]</code>	<code>a[3][2]</code>	<code>a[3][3]</code>
4	<code>a[4][0]</code>	<code>a[4][1]</code>	<code>a[4][2]</code>	<code>a[4][3]</code>
5	<code>a[5][0]</code>	<code>a[5][1]</code>	<code>a[5][2]</code>	<code>a[5][3]</code>

Viewed in this way, our two-dimensional array is a grid, much like a map or a spreadsheet. This is a natural way to store things like tables of data or matrices.

We access elements of two-dimensional arrays in a manner similar to that used for one dimensional arrays, except that we must provide both the row and column to access an element, giving the row number first.

We create a two-dimensional array by providing the number of rows and columns. Thus we can create the two-dimensional array above by writing:

```
int[][] a = new int[6][4];
```

(Though as good programmers, you would define constants for the number of rows and the number of columns.)

A nested `for` loop is the most common way to access or update the elements of a two-dimensional array. One loop walks through the rows and the other walks through the columns. For example, if we wanted to assign a unique number to each cell of our two-dimensional array, we could do the following:

```
for (int row = 0; row < 6; row++) {
    for (int col = 0; col < 4; col++) {
        a[row][col] = 4*row + col + 1;
    }
}
```

This assigns the numbers 1 through 24 to the elements of array `a`. The array is filled by assigning values to the elements in the first row, then the second row, etc. and results in:

```
1  2  3  4
5  6  7  8
9 10 11 12
13 14 15 16
17 18 19 20
21 22 23 24
```

And if we wanted to print the above, we can write a loop:

```
for (int row = 0; row < 6; row++) {
    for (int col = 0; col < 4; col++) {
        System.out.print(a[row][col] + " ");
    }
    System.out.println();
}
```

You could modify the above to be slightly more interesting by computing a multiplication table.

We could just as well process all the elements of column 0 first, then all of column 1, etc., by swapping the order of our loops:

```
for (int col = 0; col < 4; col++)
    for (int row = 0; row < 6; row++)
        ...
```

For the most part, it doesn't matter which order you choose, though for large arrays it is generally a good idea to traverse the array in the same order that your programming language will store the values in memory. For Java (and C, C++), the data is stored by rows, known as *row major* order. However, a two-dimensional array in FORTRAN is stored in *column major* order. You will almost certainly see this again if you go on and take courses like Computer Organization or Operating Systems.

Let's look at an example that makes use of a small (3×3) two-dimensional array: a tic-tac-toe game.

See Example: TicTacToe

Most of the program is pretty straightforward, so we'll focus on the use of the two-dimensional arrays and discuss some of the private helper methods that make the code simpler, especially when checking for winning boards.

The array that represents the board is a two-dimensional array of `int` called `marks`. Each entry will contain one of three values that will indicate if the cell is empty (0), contains an X (1) or contains an O (2). Named constants make the code involving these numbers easier to understand.

Several private helper methods are provided to draw the board and the X's and O's. Look a bit at the `onMousePress` method, where the game is played. When the mouse is pressed and it is determined which (if any) of the 9 spaces contain the press point, we check to see if the space is occupied. If not, the array entry is set and the appropriate mark is drawn on the screen.

From there, the `checkGameWon` method is called to see if this last move led to a win. If not, we call the `checkAllFilled` method to see if all squares are now occupied, meaning the game ends in a tie.

A hopefully more interesting use of two-dimensional arrays is to manage the bricks in a breakout game.

See Example: Breakout

This is a greatly-enhanced version of our last pong game, where there are now a series of bricks that get removed as the ball bounces off one of them.

The most relevant to the current discussion is the two-dimensional array in the `BrickCollection` class. For the game as written, the bricks could be stored in a one-dimensional array or even an `ArrayList`. However, by storing them in a two-dimensional array, we can have the additional

information about the positions if we wanted to enhance the game to have different point values based on position, for example.

Two-Dimensional Matrices

A very common use of multi-dimensional arrays is the representation of *matrices*. We will look at an example of a class that represents two-dimensional square matrices and provides some basic operations on them.

See Example: Matrix2D

The class is capable of holding a square matrix of `double` values of any positive dimension.

Comments within the example explain much of what is happening. Note in particular the use of the two-dimensional array as an instance variable which stores the matrix entries, the use of exceptions to handle error conditions, and the `main` method that tests out the methods of the class.